Shouldn't the algorithm run slower or be equal to?
So false?

Correct.

Big omega does mean they can be equal. So there could be two functions f and g which run in the same amount of time.